

## Introduction

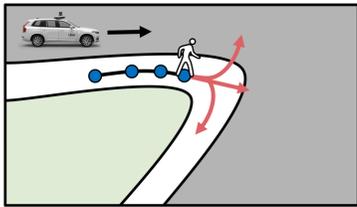
**Goal:** Forecast future pedestrian spatial occupancy over long horizon (10 seconds) in cities

**Motivation:** Safe motion planning in self-driving

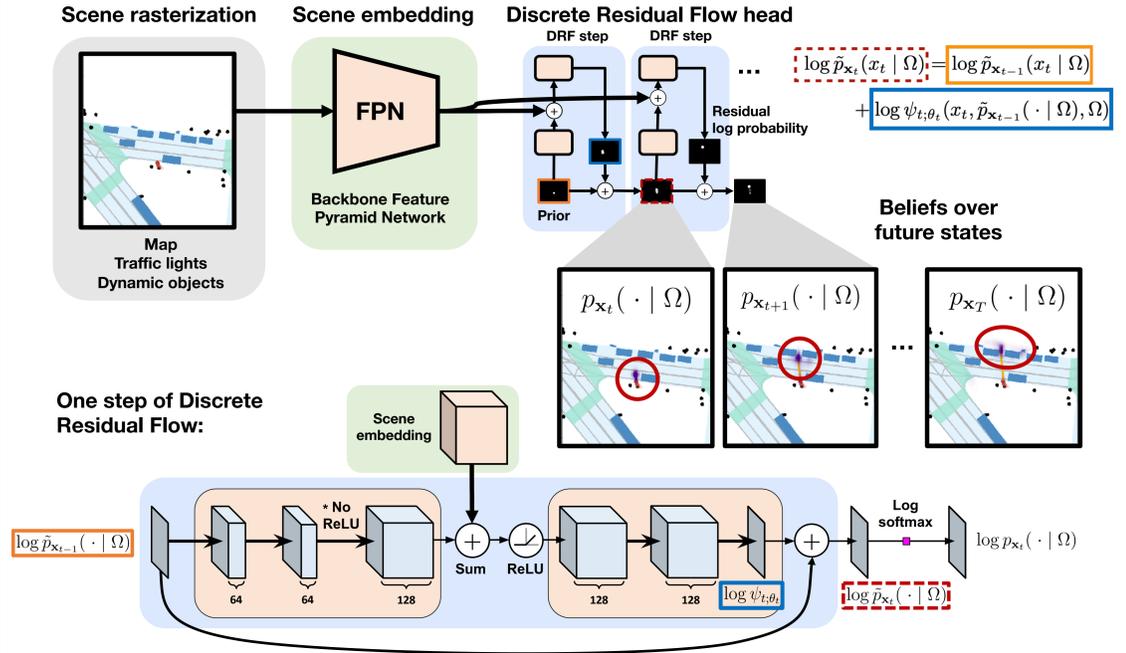
**Input:** Semantic map, dynamic actor tracks

**Challenges:**

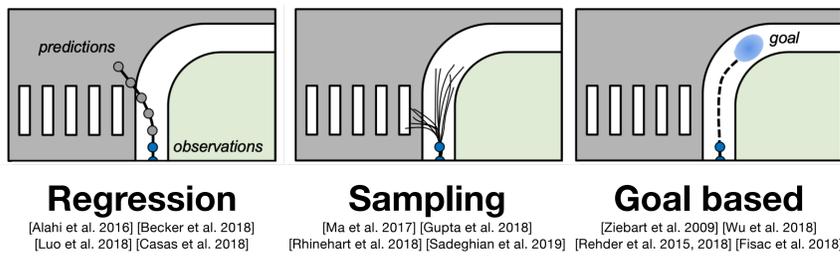
- Multiple intentions
- Significant uncertainty
- Partial observability
- Non-gaussian posteriors
- Spatiotemporal inputs



## Network architecture



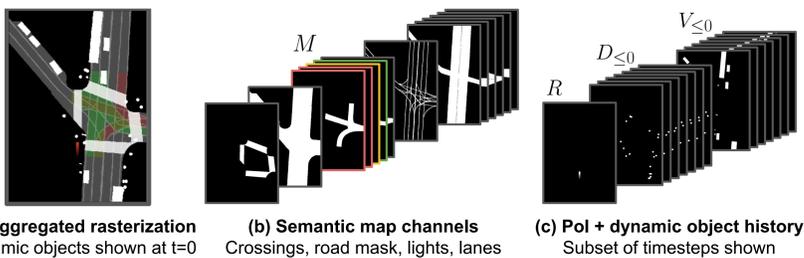
## Prior approaches



## Our approach

### Multiscale scene embedding

- Spatiotemporal feature extraction from BEV scene raster with feature pyramid network



### Probabilistic motion forecasting

- Predict marginal occupancy distributions
- Categorical predictions** are flexible, multimodal

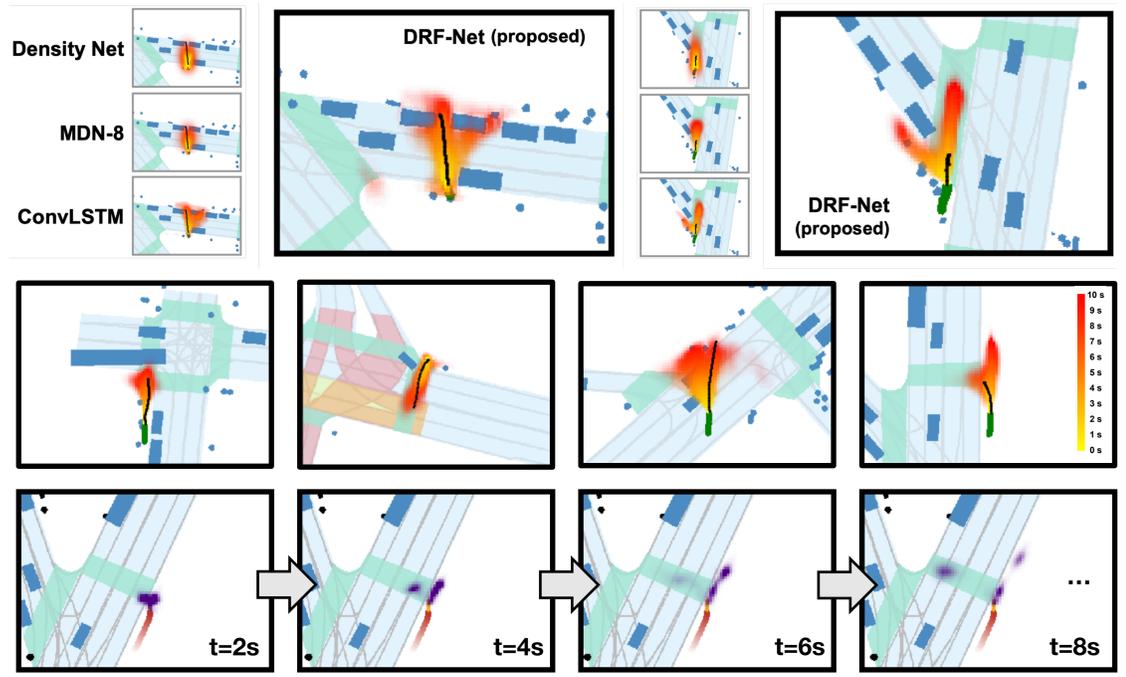
Bayesian approach: Learn conditional distributions and marginalize  $\rightarrow O(K^2)$  cost per timestep for  $K$  bins

$$p_{x_t}(x_t | \Omega) = \sum_{x_{t-1}} p_{x_t|x_{t-1}}(x_t | x_{t-1}, \Omega) p_{x_{t-1}}(x_{t-1} | \Omega)$$

DRF-NET (ours): Approximate intractable marginalization using function approximator, amortizing cost  $\rightarrow O(K)$  probability flow that predicts a residual update to previous timestep marginal

$$p_{x_t}(x_t | \Omega) = \left[ \sum_{x_{t-1}} \frac{p_{x_t|x_{t-1}}(x_t | x_{t-1}, \Omega) p_{x_{t-1}}(x_{t-1} | \Omega)}{p_{x_{t-1}}(x_{t-1} | \Omega)} \right] p_{x_{t-1}}(x_{t-1} | \Omega) \approx \frac{1}{Z_t} \underbrace{\psi_{t;\theta_t}(x_t, p_{x_{t-1}}(\cdot | \Omega), \Omega)}_{\text{Exponentiated residual}} p_{x_{t-1}}(x_{t-1} | \Omega)$$

## Qualitative results



## Evaluation

Model	Negative log likelihood (NLL)				ADE (m)				FDE (m)				Mass Ratio (%)		Real detection data (NLL)			
	Mean	@ 1 s	@ 3 s	@ 10 s	0.2-10s	@ 1 s	@ 3 s	@ 10 s	Acc.	Recall	Mean	@ 1 s	@ 3 s	@ 10 s				
Density Net	5.39	2.87	3.96	6.74	3.49	0.93	1.72	7.66	77.99	81.33	5.64	1.88	4.12	7.91				
MDN-4	3.01	1.64	2.00	4.33	1.47	0.38	0.69	3.38	87.85	84.12	3.21	1.52	2.54	4.71				
MDN-8	3.43	1.60	2.77	4.79	1.78	0.60	0.88	3.91	85.56	84.19	3.21	1.53	2.55	4.73				
ConvLSTM	2.51	0.89	1.86	4.07	1.58	0.47	1.06	3.20	88.02	85.02	3.14	1.54	2.51	4.64				
DRF-NET	<b>2.37</b>	<b>0.76</b>	<b>1.74</b>	<b>3.83</b>	<b>1.23</b>	<b>0.35</b>	<b>0.62</b>	<b>2.71</b>	<b>89.78</b>	<b>85.41</b>	<b>2.98</b>	<b>1.47</b>	<b>2.39</b>	<b>4.36</b>				

